



[+] Symbols

[-] Rules for Sentential Logic

NOTE: the order in which rule lines are cited is important for multi-line rules. For example, in an application of conditional elimination with citation "j,k \rightarrow E", line j must be the conditional, and line k must be its antecedent, *even if* line k actually *precedes* line j in the proof. The only multi-line rules which are set up so that order doesn't matter are &I and \perp I.

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